String matching
Data Structures and Algorithms for Computational Linguistics III (ISCL-BA-07)

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Finding patterns in a string
-Finding a pattern in a larger text is a common problem in many applications

- Typical example is searching in a text editor or word processor

There are many more:

- DNA sequencing / bioinformatics
- Plagiarism detection
- Seart engines / information retrieval
- Spell checking


## Types of problems

- The efficiency and usability of al gorithms depend on some properties of the problem
- Typical applications are based on finding multiple occurrences of a single pattern in a text, where the pattern is much shorter than the text
The efficiency of the algorithms may depend on the
- relative size of the pattern
- expected number of repetitions
whether the pattern
解 the pattern is used once or many times
Another related problem is searching for multiple patterns at once
In some cases, fuzzy / approximate search may be required
- In some applications, preprocessing (indexing) the text to be searched may be beneficial
$\qquad$

Brute-force string search


- Start from the beginning, of $\mathrm{i}=0$ and $\mathrm{j}=0$
- if $f=m$, announce success with $s=i$
- otherwise: compare the next character (increase $i$ and $j$, repeat)


## Brute-force string search



```
p: \(\quad\)\begin{tabular}{|c|c|c|c|}
\hline A & G & C & A \\
\hline 10 & 1 & 2 & 3 \\
\hline
\end{tabular}
```

- Start from the beginning, of $\mathrm{i}=0$ and $\mathrm{j}=0$
- if $j==m$, announce success with $s=i$

- otherwise: compare the next character (increase $i$ and $j$, repeat)
$\qquad$


## Brute-force string search



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- if $j==m$, announce succees with $s=i$
- if $t(i)=p(j)$ : shift $p$ (increase $i$, set $j=0)$
- otherwise: compare the next character (increase $t$ and j , repeat)

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Start from the beginning, of $i=0$ and $j=0$

- if $j=m$, announce success with $s=i$
- if $t i i)=p \mid j$ : shift $p$ (increase $i$, set $j=0$ )
- otherwise: compare the next character (increase $t$ and $\mathfrak{j}$, repeat)


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## Brute-force string search

```
\begin{tabular}{|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|}
\hline A & A & T & A & G & A & C & G & G & C & T & A & G & C & A & A \\
\hline
\end{tabular}
\(p:\)
\begin{tabular}{|l|l|l|l|}
\hline A & G & C & A \\
\hline 0 & 1 & 2 & 3 \\
\hline
\end{tabular}
```

Start from the beginning, of $\mathrm{i}=0$ and $\mathrm{j}=0$

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- otherwise: compare the next character (increase $i$ and $j$, repeat)

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Brute-force string search

| A | A | T | A | G | A | C | G | G | C | T | A | G | C | A | A |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

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Brute-force string search


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Brute-force string search

```
\begin{tabular}{|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|l|}
\hline A & A & T & A & G & A & C & G & G & C & T & A & G & C & A & A \\
\hline
\end{tabular}
\(p\).
```

\section*{|  |  | C |  |
| :---: | :---: | :---: | :---: |}

Start from the beginning, of $i=0$ and $j=0$

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- if $j==$ m, announce success with $s=i$
- if $\mathrm{ti} \mathrm{i}=\mathrm{p}[\mathrm{j}]$ : shift p (increase i , set $\mathrm{j}=0$ )
- otherwise: compare the next character (increase $i$ and $j$, repeat)
 $\qquad$

Brute-force string search


| A | A | T | A | G | A | C | G | G | C | T | A | G | C | A | A |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$p$ :


- Start from the beginning, of $\mathrm{i}=0$ and $\mathrm{j}=0$
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Brute-force string search


- Start from the beginning, of $i=0$ and $j=0$

- otherwise: compare the next character (increase $i$ and $j$, repeat)

```
Brute-force string search
```



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- otherwise: compare the next character (increase $i$ and $j$, repeat)


Brute-force string search

t: | A | A | T | A | G | A | C | G | G | C | T | A | G | C | A | A |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$p$ :


## Brute-force approach: worst case




Brute-force approach: worst case


## Brute-force approach: worst case



## Brute-force approach: worst case



Brute-force approach: worst case


Brute-force approach: worst case

 | 1 | 1 | 1 |
| :--- | :--- | :--- | :--- |
|  | 1 | 1 |

$p$. | A | A | A | C |
| :--- | :--- | :--- | :--- |
| D | 1 | 2 | 3 |




Brute-force approach: worst case



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Brute-force approach: worst case

t. $\quad$| 16 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | A | A | A | A | A | A | A | A | A | A | A | A | A | A | A | C |



Brute-force approach: worst case


Brute-force approach: worst case
 $p$ p

## Brute-force approach: worst case




Brute-force approach: worst case


Boyer-Moore algorithm
slightly simplified verson


p: $\quad$| A | G | A | C |
| :---: | :---: | :---: | :---: |
|  | 0 | 1 | 2 |

- The main idea is to start comparing from the end of $p$

If $t(i)$ does not occur in $p$, shift $m$ steps
Otherwise, align the last occurrence of $t[i]$ in $p$ with $t[i]$

## Boyer-Moore algorithm

slighty simplified versum


p. $\quad$| A | G | A | C |
| :--- | :--- | :--- | :--- |
| $\quad 0$ | 0 | 1 | 2 |

The main idea is to start comparing from the end of $p$
If $t$ li does not occur in $p$, shift $m$ steps
Otherwise, align the last occurrence of $t[i]$ in $p$ with $t[i]$

Brute-force approach: worst case


- Worst-case complexity of the method is $\mathrm{O}(\mathrm{nm})$
- Crucially, most of the comparisons are redundant
for $i>0$ and any comparison with $j=0,1,2$, we already inspected corresponding ivalues
The main idea for more advanced algorithms is to avoid this unnecessary comparisons

Boyer-Moore algorithm
slighty smplified verston


The main idea is to start comparing from the end of $p$
If $t \mathrm{i}$ does not occur in $p$, shift $m$ steps

- Otherwise, align the last occurrence of $t[i]$ in $p$ with $t[i]$

Boyer-Moore algorithm
stighty simplifed verson


- The main idea is to start comparing from the end of $p$

If $t$ ii does not occur in $p$, shift $m$ steps

- Otherwise, align the last occurrence of $t[i]$ in $p$ with $t[i]$


Boyer-Moore algorithm
slightly simplified verson


- The main idea is to start comparing from the end of $p$
- If $t[i]$ does not occur in $p$, shift $m$ steps

Otherwise, align the last occurrence of $t[i]$ in $p$ with $t[i]$

Boyer-Moore algorithm
implementation and analysis

On average, the algorithm performs better than brute-force
In worst case the complexity of the algorithm is $\mathrm{O}(\mathrm{nm})$, example
$\mathrm{t}=\mathrm{aaa} \ldots \mathrm{a}, \mathrm{p}=\mathrm{baa} \ldots \mathrm{a}$

- Faster versions exist ( $O(n+m+q)$ )

> last - 0
> for $j$ in range( $n$ ): $1, j-n-1, m-1$
> while i $<\mathrm{n}$ :
> if $\mathrm{T}[\mathrm{i}]=\mathrm{P}[\mathrm{j}$ )
> return i
> else:
> $\stackrel{\text { alse }}{1} 1$
> else ${ }^{j}$
> $\mathrm{k}=$ last.get(T[i], -1)
> $=m+\min (j, k+1)$
> turn None


A quick introduction to FSA

- Another efficient way to search a string is building a finite state automaton for the pattern
- An FSA is a directed graph where edges have labels
- One of the states is the initial state
- Some states are accepting states
- We will study FSA more in-depth soon

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An FSA for the pattern ACGAC


- Start at state 0 , switch states based on the input
- All unspecified transitions go to state 0

When at the accepting state, announce success
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FSA pattern matching
demonstration



FSA pattern matching
demonstration



FSA pattern matching
demonstration



FSA pattern matching
demonstratom



FSA pattern matching
demonstratom



FSA pattern matching



FSA pattern matching



FSA pattern matching
demonstration



FSA pattern matching



FSA pattern matching
demonstration

| A | A | A | C | G | A | C | G | A | C | A | T | A | C | G | A | C |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |



## FSA pattern matching

demonstration

| 0 | 12 | 12 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | A | A | C | G | A | C | G | A | C | A | T | A | C | G | A | C |



FSA pattern matching
demonstratoon



FSA pattern matching
demonstration



SA pattern matching
demonstration



FSA pattern matching
demonstratoon





Knuth-Morris-Pratt (KMP) algorithm

- The KMP algorithm is probably the most popular algorithm for string matching
- The idea is similar to the FSA approach: on failure, continue comparing from the longest matched prefix so far
- However, we rely on a simpler data structure (a function/table that tells us
where to back up)
- Construction of the table is also faster


## KMP algorithm


KMP algorithm
demonstration

- In case of a match, increment both $i$ and $j$
- On failure, or at the end of the pattern, decide which new $p[j]$ compare with
$t(i)$ based on a function $f$
- $f[j-1]$ tells which $j$ value to resume the comparisons from
- In case of a match, increment both $i$ and $j$

On failure, or at the end of the pattern, decide which new p[j] compare with $t \mid i]$ based on a function $f$

- $f[j-1]$ tells which $j$ value to resume the comparisons from



## KMP algorithm <br> demanstration



- In case of a match, increment both $i$ and $j$
- On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t[i]$ based on a function $f$
- $f[j-1]$ tells which $j$ value to resume the comparisons from


## KMP algorithm

demonstration

\section*{ <br> $p$. <br> | A | C | G | A | C |
| :---: | :---: | :---: | :---: | :---: |

- In case of a match, increment both $i$ and $j$

On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t[i]$ based on a function $f$

- $f[j-1]$ tells which $j$ value to resume the comparisons from


## KMP algorithm

demonstration

| A | A | C | G | A | T | G | A | C | A | T | A | C | G | A | C | A | T | G |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | |  |  | A | C | A |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | A | C |  |
| 0 | 1 | 2 | 3 | 4 |

In case of a match, increment both i and j

- On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t[i]$ based on a function $f$
- $f[j-1]$ tells which $j$ value to resume the comparisons from


## KMP algorithm

demonstration

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  | 1 | 12 | 13 | 14 | 1. | 16 | 17 | G |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $t$ | A | A | C | G | A | T | G | A | C | A | T |  | A | C | G | A | C | A | T |  |
|  | , |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $p$. |  |  |  |  |  |  |  |  |  |  |  |  | C | G | A | C |  |  |  |  |
|  |  | 1 0 1 2 3 4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | 60 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

- In case of a match, increment both $i$ and $j$
- On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t(i)$ based on a function $f$
- $f[j-1]$ tells which $j$ value to resume the comparisons from
$t[i]$ based on a function $f$
f $j-1]$ tells which $j$ value to resume the comparisons from


## KMP algorithm

demanstration

$p$ :


- In case of a match, increment both $i$ and $j$

On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t \mid i]$ based on a function $f$

- $f[j-1]$ tells which $j$ value to resume the comparisons from

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## KMP algorithm

demonstration

 $p$. | A | C | G | A | C |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 1 | 3 | 3 |

- In case of a match, increment both $i$ and $j$

On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t$ (i) based on a function $f$

- $f[j-1]$ tells which $j$ value to resume the comparisons from

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In the while loop, we either increase $i$, or shift the comparison
As a result, the loop runs at most $2 n$ times, complexity is $\mathrm{O}(\mathrm{n})$


$\mathrm{f}=[0]$. n
$\mathrm{j} . \mathrm{k}-1,0$
while $\overline{1}<\mathrm{n}: ~$
if $P[j]=P[k]$.

$\mathrm{j}+\boldsymbol{1}$
$\mathrm{k}+\boldsymbol{1}$
$\left.\left.\begin{array}{rl}\text { elif } k>0: \\ k-f a i l\end{array}\right]-1\right]$
olse:

Building the failure table

while $j<\mathrm{n}$ :
if $P[j]-P[k]$ :
$\mathrm{f}[\mathrm{j}]=\mathrm{k}$
$\mathrm{j}+\mathrm{k}$
$\mathrm{k}+\mathrm{m}$

| A | T | A | C | G | A | T | A | C | A | T | G | C |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\uparrow$ |  |  |  |  |  |  |  |  |  |  |  |  |

elif $k>0$;

| $\begin{array}{l}k \text { k fail }[k-1] \\ \text { else: } \\ j+2\end{array} \quad f:$0 0 0 0 0 0 0 0 0 0 0 0 0 |
| :--- |

elas:

Building the failure table

$\mathrm{j}, \mathrm{k}-1.0$
while $\mathrm{j}<\mathrm{n}$
:
if $\mathrm{P}[\mathrm{j}] \mathrm{n}:-\mathrm{P}[\mathrm{k}]:$
$\mathrm{f}[\mathrm{j}]=\mathrm{k}+\mathrm{l}$
$f[j]=k+1$
$\mathrm{j}+\boldsymbol{1}$
$\mathbf{k}+\boldsymbol{1}$
elif k > 0:
k = fail $[k-1]$
elos:



$\qquad$
$\qquad$
$\mathrm{f}=[\mathrm{l}, \mathrm{n}$
$\mathrm{j}, \mathrm{k}=1$,
while $j<n:$
if $P[j]=P[k]=$
$f[j]=k+1$

p: | A | T | A | C | G | A | T | A | C | A | T | G | C |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\begin{array}{cc}\left.\begin{array}{c}k+1 \\ \text { elif } k>\end{array}\right) & \uparrow \\ k\end{array}$
$k=$ fail [k - 1]
$\stackrel{\text { else: }}{j+1}$



Building the failure table
$\mathrm{f}=[0]=\mathrm{n}$
$\mathrm{j}, \mathrm{k}=1,0$
while $j<n: 8[k]$ :
$\underset{\substack{f \\ j \\ j+\infty \\ j \\ j}}{ }=k+$

elif $k>0:$
$k=$ fail $[k-1]$
else:
else:
$j+\infty$
+



Building the failure table

|  | j |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\text { if } P[j]-P[k] \text { : }$ |  |  | T | A | C | G | A | T | A | C | A | I | c |  | C |
| $\mathrm{j}+\infty$ | k |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| olif $k>0$ : |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| else: |  |  | 0 | 1 | 0 | 0 | 1 | 2 | 3 | 4 | 0 | 0 | 0 |  | 0 |



Building the failure table
f $-\mathrm{L0}$ ] $=\mathrm{n}$
$\mathrm{j}, \mathrm{k}-1,0$
while $j<\mathrm{n}:$
if $\begin{gathered}\mathrm{P}[\mathrm{j}] \\ \mathrm{f}[\mathrm{j}]\end{gathered} \mathrm{m}+\mathrm{p}[\mathrm{k}]=$
$\sum_{\substack{+\infty \\ k+\infty}}$
elif $k>0$ :
$k-$ fail $[k-1]$
else:
$j$


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$\underset{f}{\mathrm{f}}[\mathrm{j}]-k+1$
$j_{k+1}^{+2}$
$k^{+-1}$
elif $k>0:$
$k-$ fail $[k-1]$
els:
$\stackrel{\text { else: }}{\substack{\text { + }}}$


Building the failure table

Building the failure table



Building the failure table

$$
\begin{aligned}
& \begin{array}{l}
\mathrm{f}=[\mathrm{e}]+\mathrm{n} \\
\mathrm{j}, \mathrm{k}=1,
\end{array}
\end{aligned}
$$

> if $f[j]-k+1$
> $\begin{aligned} & \mathrm{j}+\mathrm{+} \\ & \mathrm{k}+1\end{aligned}$
> $\begin{aligned} & \text { elif } k>0: \\ & k \text { fand }[k-1] \\ & \text { else: }\end{aligned}$
> j+-

2

uilding the failure table
$\mathrm{f}-\mathrm{Loj}, \mathrm{n}$
$\mathrm{j}, \mathrm{k}=1,0$
while $j<n:$
if $P[j]-P[k]=$
${ }_{f} f[j]=k+1$
$j+1$
$k+-1$

elif $k>0:$
$k=$ fail $[k-1]$
elas:
j+

## Rabin-Karp algorithm

- Rabin-Karp string matching algorithm is another interesting algorithm
- The idea is instead of matching the string itself, matching the hash of it (based on a hash function)
If a match found, we need to verify - the match may be because of a hash collision
Otherwise, the algorithm makes a single comparison for each position in the text
However, a hash should be computed for each position (with size m)
- Rolling hash functions avoid this complication


## Rabin-Karp string matching

demonstration with additive haching


\section*{$p:$| 4 | 3 | 8 | 5 | 7 | 9 | 4 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |$\quad h(p)=43$}

A rolling hash function changes the hash value only based on the item coming in and going out of the window

- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Rabin-Karp string matching
demonstration with additive hasting

\section*{t: | 7 | 1 | 3 | 6 | 7 | 4 | 3 | 8 | 5 | 7 | 9 | 4 | 3 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | <br> $h=37$}


\section*{$p:$| 4 | 3 | 8 | 5 | 7 | 9 | 4 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |$\quad \mathrm{~h}(\mathrm{p})=43$}

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Rabin-Karp string matching
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| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |$\quad h(p)=43$}

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Rabin-Karp string matching
demonstration with additive hashing


\section*{$p:$| 4 | 3 | 8 | 5 | 7 | 9 | 4 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |$\quad \mathrm{~h}(\mathrm{p})=43$}

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g.. polynomial hash functions) can also be used

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Rabin-Karp string matching
demonstration with additive hashing


\section*{$p:$| 4 | 3 | 8 | 5 | 7 | 9 | 4 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |$\quad \mathrm{~h}(\mathrm{p})=43$}

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## Summary

- String matching is an important problem with wide range of applications
- The choice of algorithm largely depends on the problem
- We will revisit the problem on regular expressions and finite-state automata
- Reading: Goodrich, Tamassia, and Goldwasser (2013, chapter 13) Next:
- Algorithms on strings: edit distance / alignment
- Reading: Goodrich, Tamassia, and Goldwasser (2013, chapter 13)Jurafsky and Martin (2009, section 3.11, or 2.5 in online draft)

Acknowledgments, credits, references

目 Goodrich, Michael T., Roberto Tamassia, and Michael H. Goldwasser (2013)Data Structures and Algorithms in Python. John Wiley \& Sons, Incorporated. ISBN 9781118476734 Jurafsky, Daniel and James H. Martin (2009). Speech and Language Processing: An Introduction to Natuml Language Processing, Computational Linguistics, and Speech Recognition. second edition. Pearson Prentice Hall. Isen: 978-0-13-504196-3.


